

***High Speed Communication Circuits and Systems***  
***Lecture 6***  
***Enhancement Techniques for Broadband Amplifiers,  
Narrowband Amplifiers***

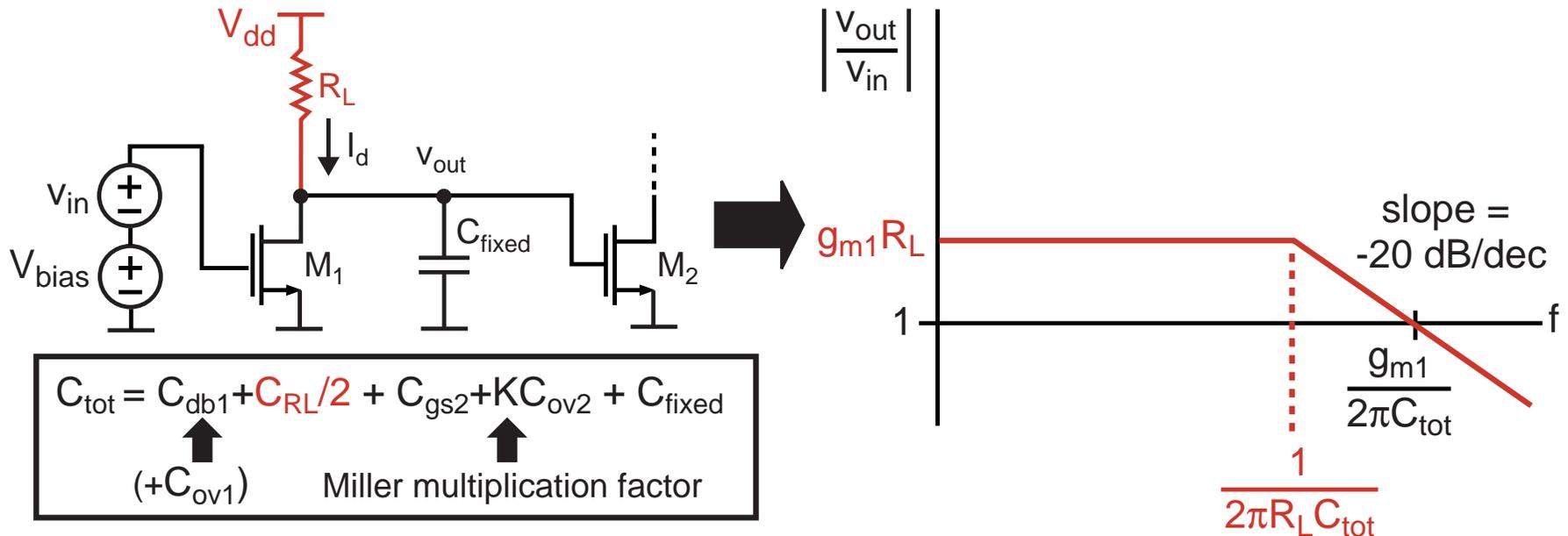
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**February 20, 2004**

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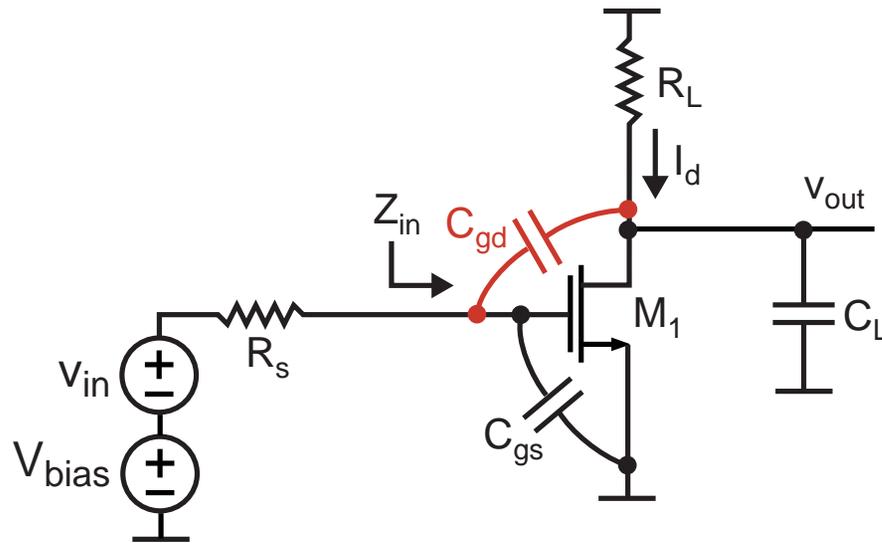
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# Resistor Loaded Amplifier (Unsilicided Poly)



- We decided this was the fastest non-enhanced amplifier
  - Can we go faster? (i.e., can we enhance its bandwidth?)
- We will look at the following
  - Reduction of Miller effect on  $C_{gd}$
  - Shunt, series, and zero peaking
  - Distributed amplification

## Miller Effect on $C_{gd}$ Is Significant



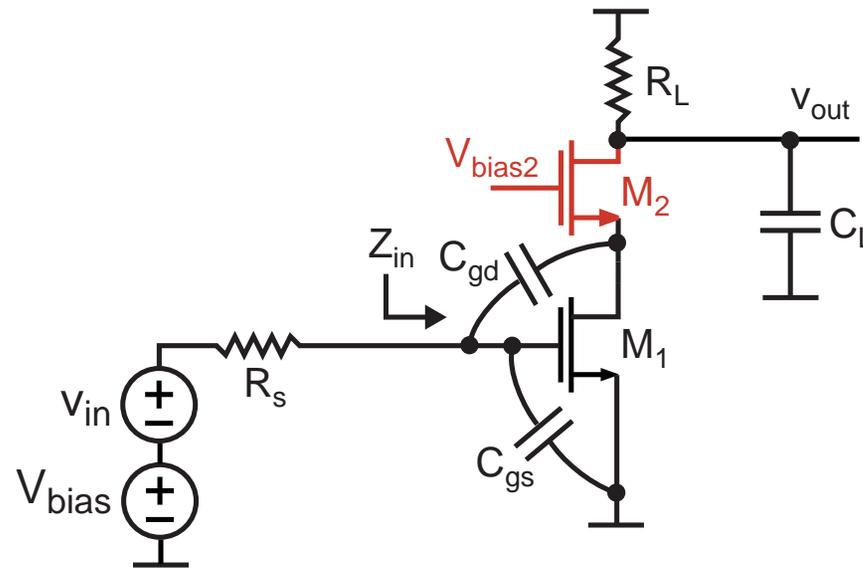
- $C_{gd}$  is quite significant compared to  $C_{gs}$ 
  - In  $0.18\mu$  CMOS,  $C_{gd}$  is about 45% the value of  $C_{gs}$
- Input capacitance calculation

$$Z_{in} \approx \frac{1}{s(C_{gs} + C_{gd}(1 - A_v))} = \frac{1}{sC_{gs}(1 + C_{gd}/C_{gs}(1 + g_m R_L))}$$

- For  $0.18\mu$  CMOS, gain of 3, input cap is almost tripled over  $C_{gs}$ !

$$Z_{in} \approx \frac{1}{sC_{gs}(1 + 0.45(4))} = \frac{1}{sC_{gs}2.8}$$

# Reduction of $C_{gd}$ Impact Using a Cascode Device



- The cascode device lowers the gain seen by  $C_{gd}$  of  $M_1$

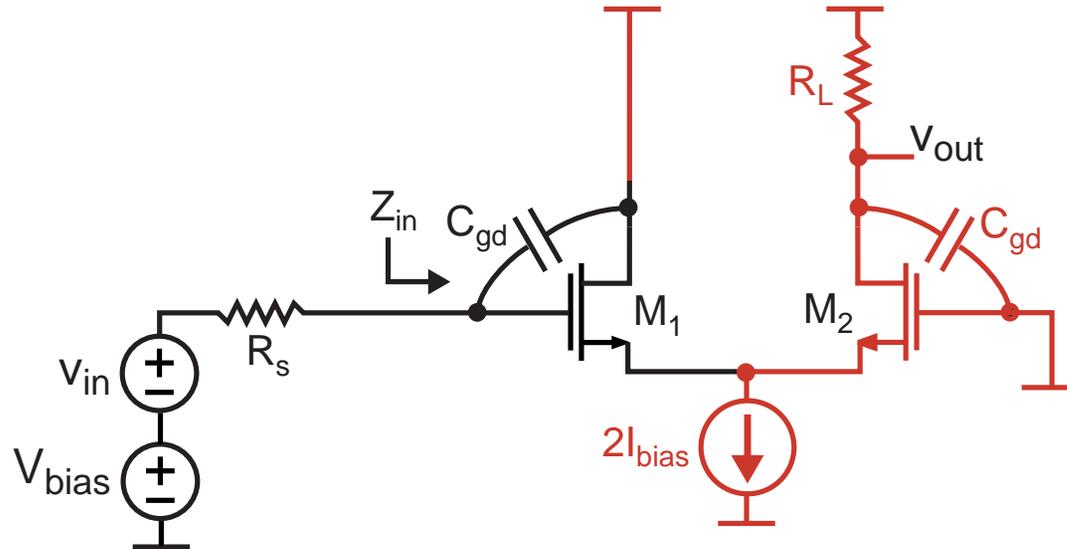
$$A_v \rightarrow g_{m1} \frac{1}{g_{m2}} \approx 1 \Rightarrow Z_{in} \approx \frac{1}{sC_{gs}(1 + C_{gd}/C_{gs}(2))}$$

- For 0.18m CMOS and gain of 3, impact of  $C_{gd}$  is reduced by 30%:

$$Z_{in} \approx \frac{1}{sC_{gs}1.9}$$

- Issue: cascoding lowers achievable voltage swing

# Source-Coupled Amplifier

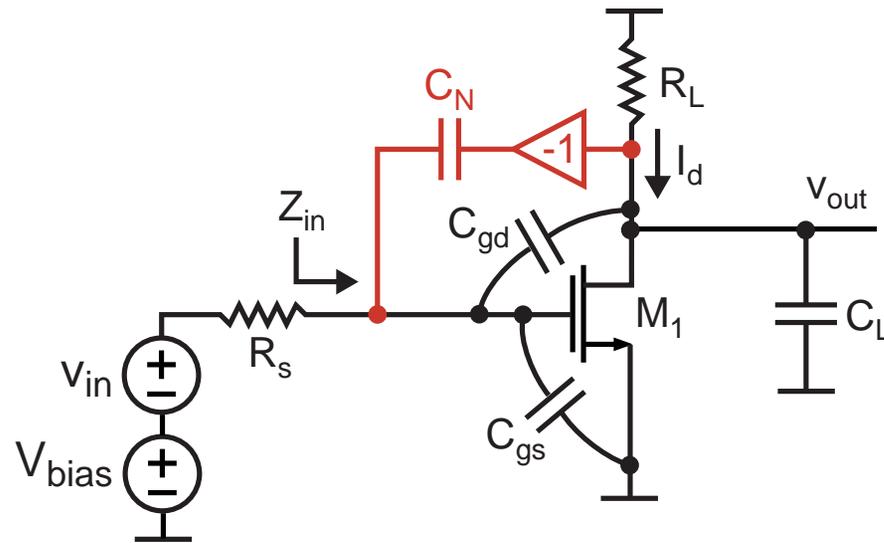


- **Remove impact of Miller effect by sending signal through source node rather than drain node**
  - $C_{gd}$  not Miller multiplied AND impact of  $C_{gs}$  cut in half!

$$Z_{in} \approx \frac{1}{s(C_{gs}/2 + C_{gd})} \Rightarrow Z_{in} \approx \frac{1}{sC_{gs}0.95} \quad (0.18\mu \text{ CMOS})$$

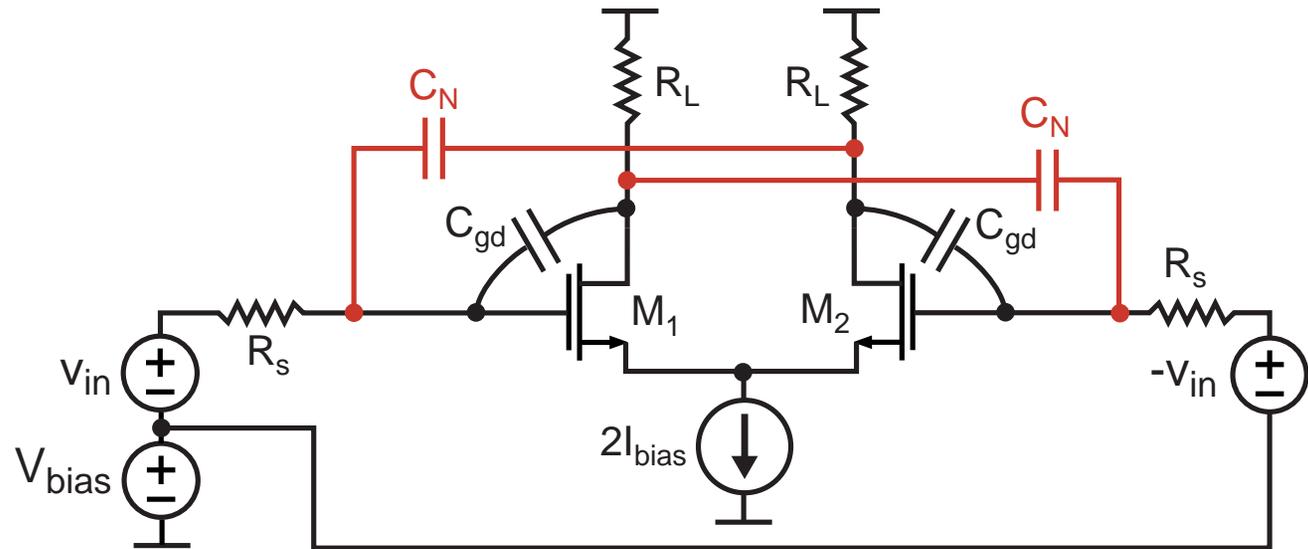
- **The bad news**
  - Signal has to go through source node ( $C_{sb}$  significant)
  - Power consumption doubled

# Neutralization



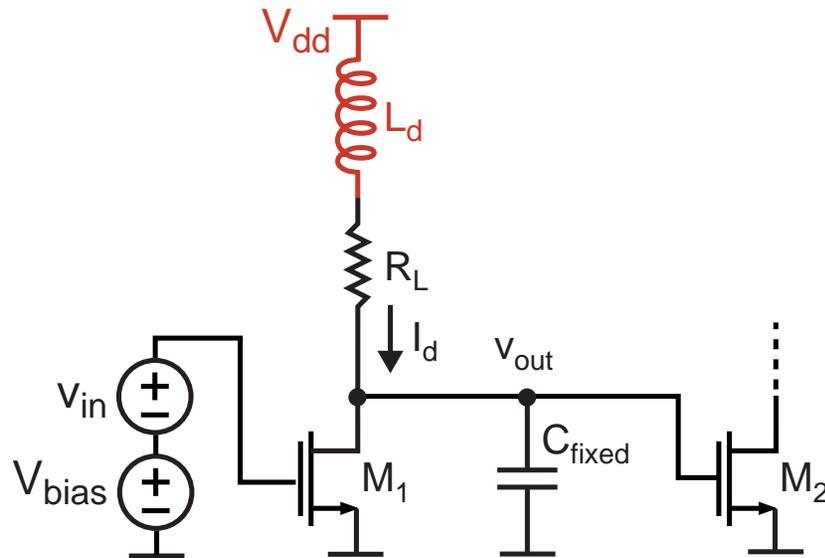
- **Consider canceling the effect of  $C_{gd}$** 
  - Choose  $C_N = C_{gd}$
  - Charging of  $C_{gd}$  now provided by  $C_N$
- **Benefit: Impact of  $C_{gd}$  removed**  $\Rightarrow Z_{in} \approx \frac{1}{sC_{gs}}$
- **Issues:**
  - How do we create the inverting amplifier?
  - What happens if  $C_N$  is not precisely matched to  $C_{gd}$ ?

# Practical Implementation of Neutralization



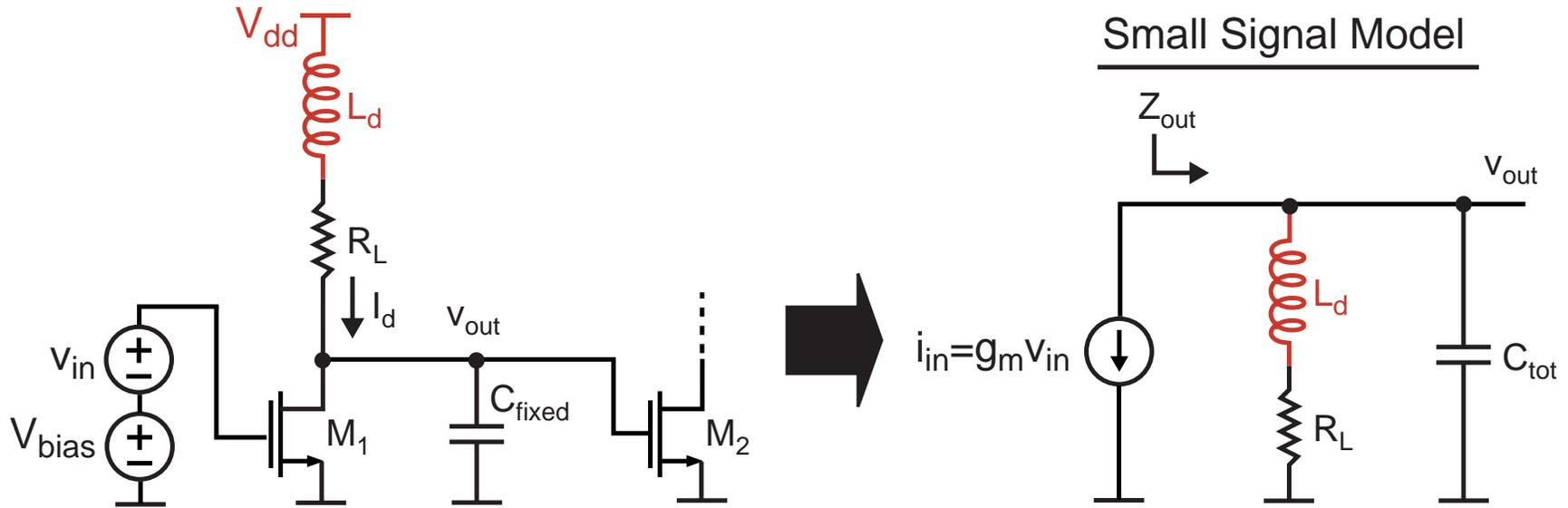
- Leverage differential signaling to create an inverted signal
- Only issue left is matching  $C_N$  to  $C_{gd}$ 
  - Often use lateral metal caps for  $C_N$  (or CMOS transistor)
  - If  $C_N$  too low, residual influence of  $C_{gd}$
  - If  $C_N$  too high, input impedance has inductive component
    - Causes peaking in frequency response
    - Often evaluate acceptable level of peaking using eye diagrams

# Shunt-peaked Amplifier



- **Use inductor in load to extend bandwidth**
  - Often implemented as a spiral inductor
- **We can view impact of inductor in both time and frequency**
  - In frequency: peaking of frequency response
  - In time: delay of changing current in  $R_L$
- **Issue – can we extend bandwidth without significant peaking?**

# Shunt-peaked Amplifier - Analysis



- **Expression for gain**

$$A_v = g_m Z_{out} = g_m [(sL_d + R_L) || 1/(sC_{tot})]$$

- **Parameterize with**

$$= g_m R_L \frac{s(L_d/R_L) + 1}{s^2 L_d C_{tot} + s R_L C_{tot} + 1}$$

$$m = \frac{R_L C_{tot}}{\tau}, \quad \text{where } \tau = \frac{L_d}{R_L}$$

- **Corresponds to ratio of RC to LR time constants**

# The Impact of Choosing Different Values of $m$ – Part 1

- Parameterized gain expression

$$A_v = g_m R_L \frac{\tau s + 1}{s^2 \tau^2 m + s \tau m + 1}$$

- Comparison of new and old 3 dB frequencies

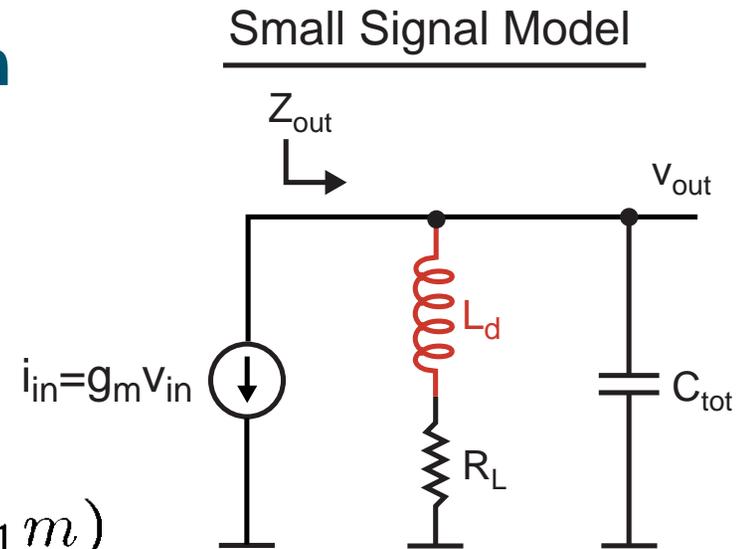
set:  $s = j\omega, \omega_1 = \frac{1}{RC}, \tau = 1/(\omega_1 m)$

$$|A_v| = g_m R_L \left| \frac{j\omega/(\omega_1 m) + 1}{-(\omega/(\omega_1 m))^2 m + j\omega/(\omega_1 m)m + 1} \right|$$

define  $\omega_2$  as new 3 dB frequency, note that  $\omega_1$  is old one

$$\Rightarrow \left| \frac{j\omega_2/(\omega_1 m) + 1}{-(\omega_2/(\omega_1 m))^2 m + j\omega_2/\omega_1 + 1} \right| = \frac{1}{\sqrt{2}}$$

- Want to solve for  $\omega_2/\omega_1$



## The Impact of Choosing Different Values of $m$ – Part 2

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- From previous slide, we have

$$\left| \frac{j\omega_2 / (\omega_1 m) + 1}{-(\omega_2 / (\omega_1 m))^2 m + j\omega_2 / \omega_1 + 1} \right| = \frac{1}{\sqrt{2}}$$

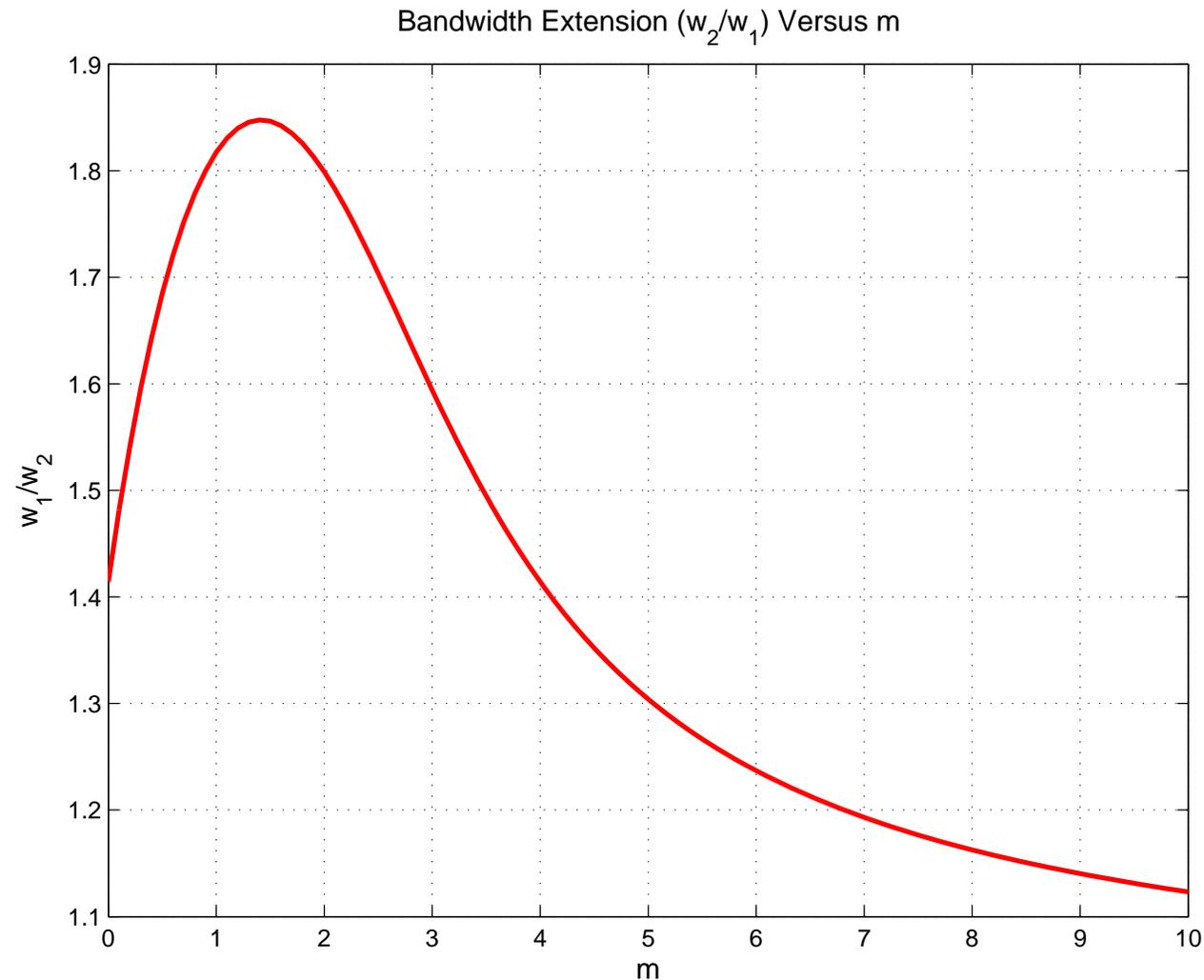
- After much algebra

$$\frac{\omega_2}{\omega_1} = \sqrt{\left(-\frac{m^2}{2} + m + 1\right)} + \sqrt{\left(-\left(\frac{m^2}{2} + m + 1\right)^2 + m^2\right)}$$

- We see that  $m$  directly sets the amount of bandwidth extension!
  - Once  $m$  is chosen, inductor value is

$$L_d = \frac{R_L^2 C_{tot}}{m}$$

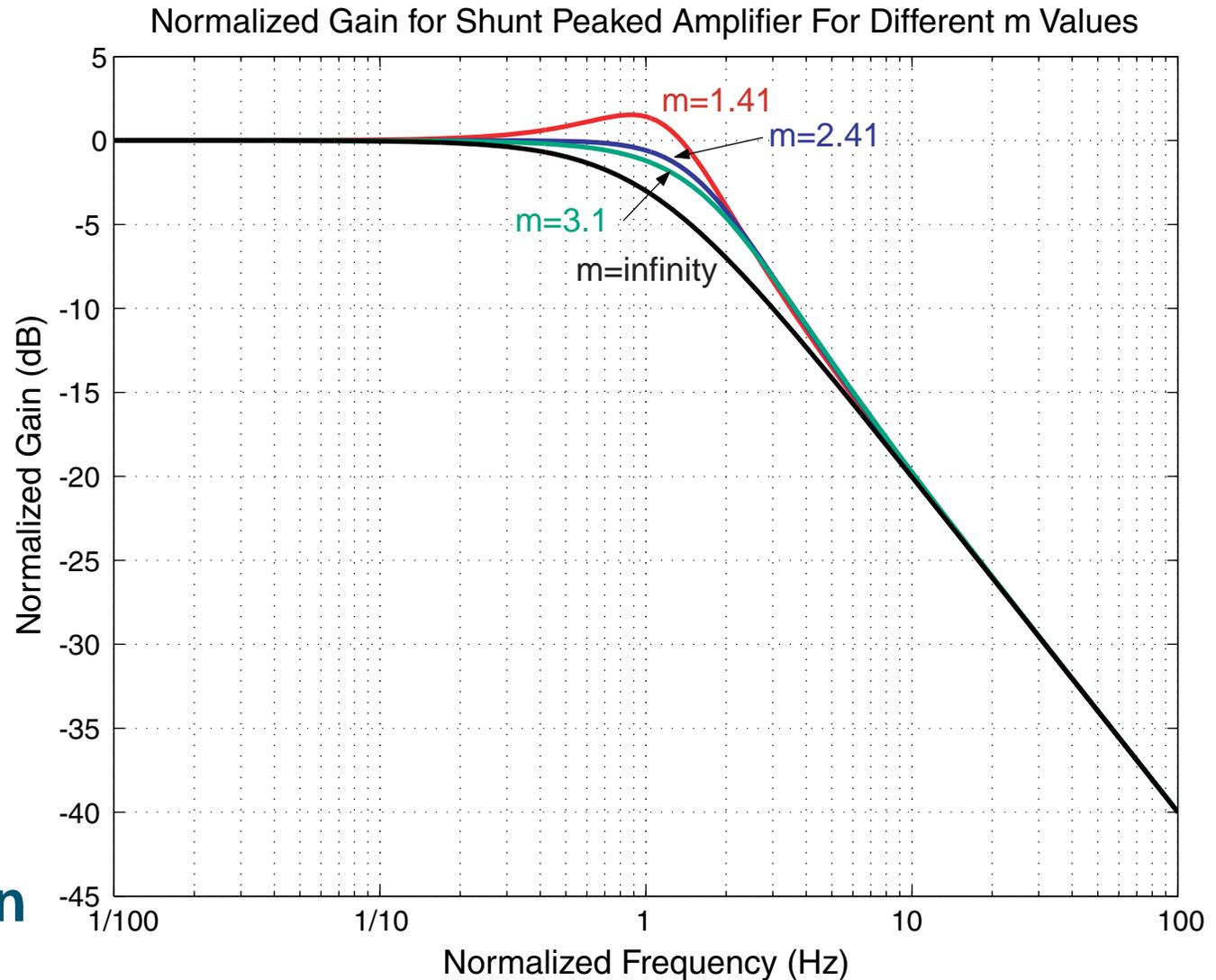
# Plot of Bandwidth Extension Versus $m$



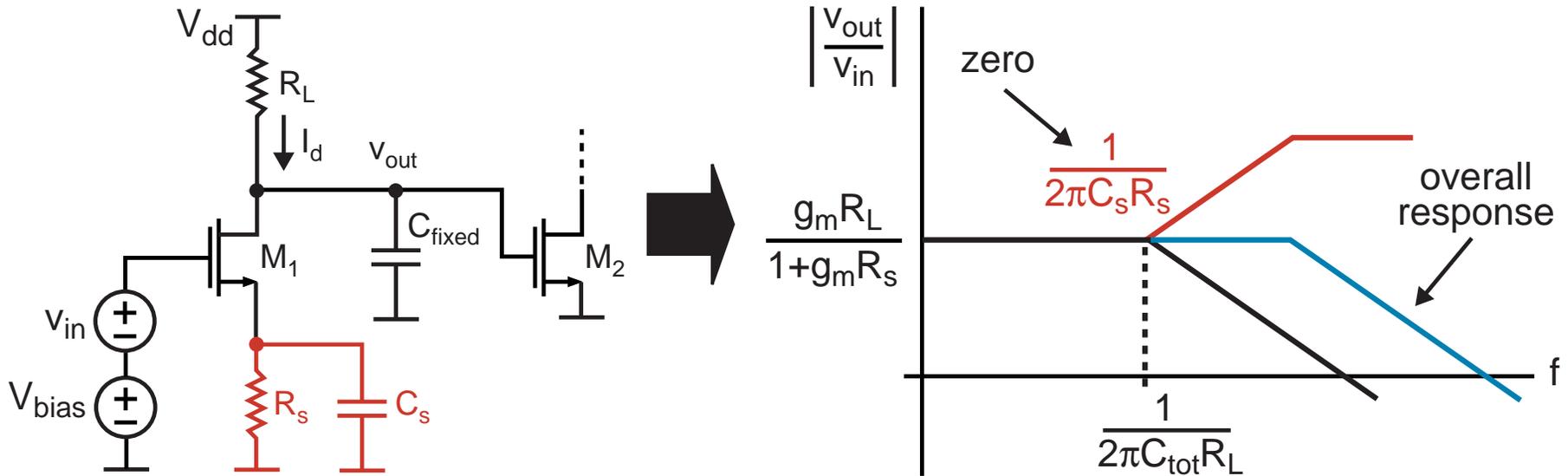
- Highest extension:  $w_2/w_1 = 1.85$  at  $m \approx 1.41$ 
  - However, peaking occurs!

# Plot of Transfer Function Versus $m$

- **Maximum bandwidth:**  
 $m = 1.41$   
(extension = 1.85)
- **Maximally flat response:**  
 $m = 2.41$   
(extension = 1.72)
- **Best phase response:**  
 $m = 3.1$   
(extension = 1.6)
- **No peaking:**  
 $m = \text{infinity}$
- **Eye diagrams often used to evaluate best  $m$**

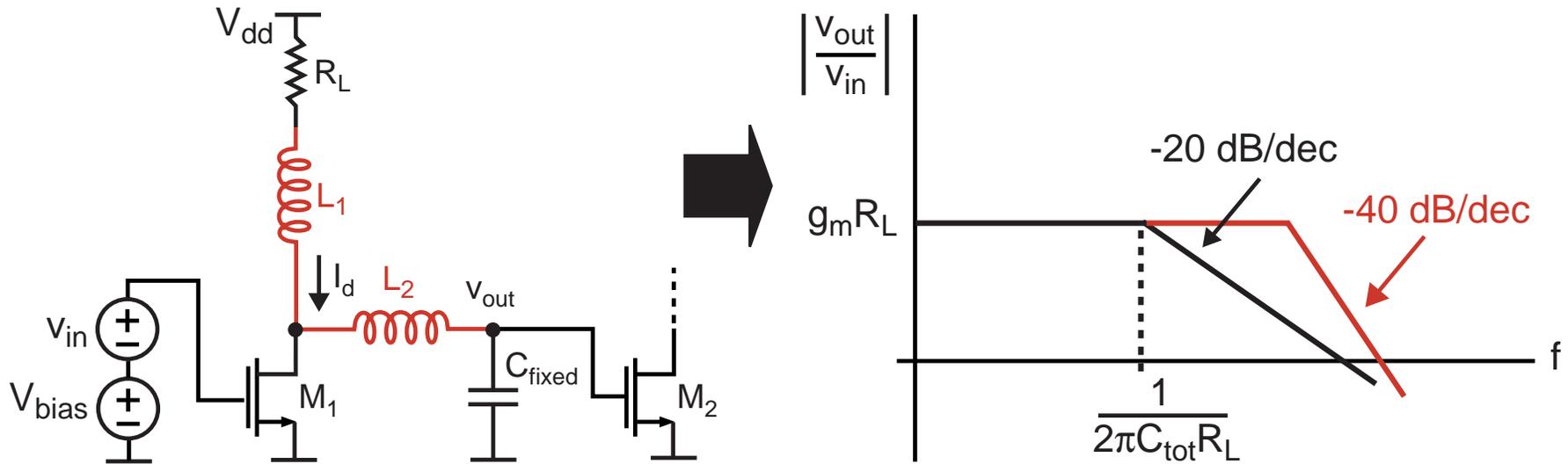


# Zero-peaked Common Source Amplifier



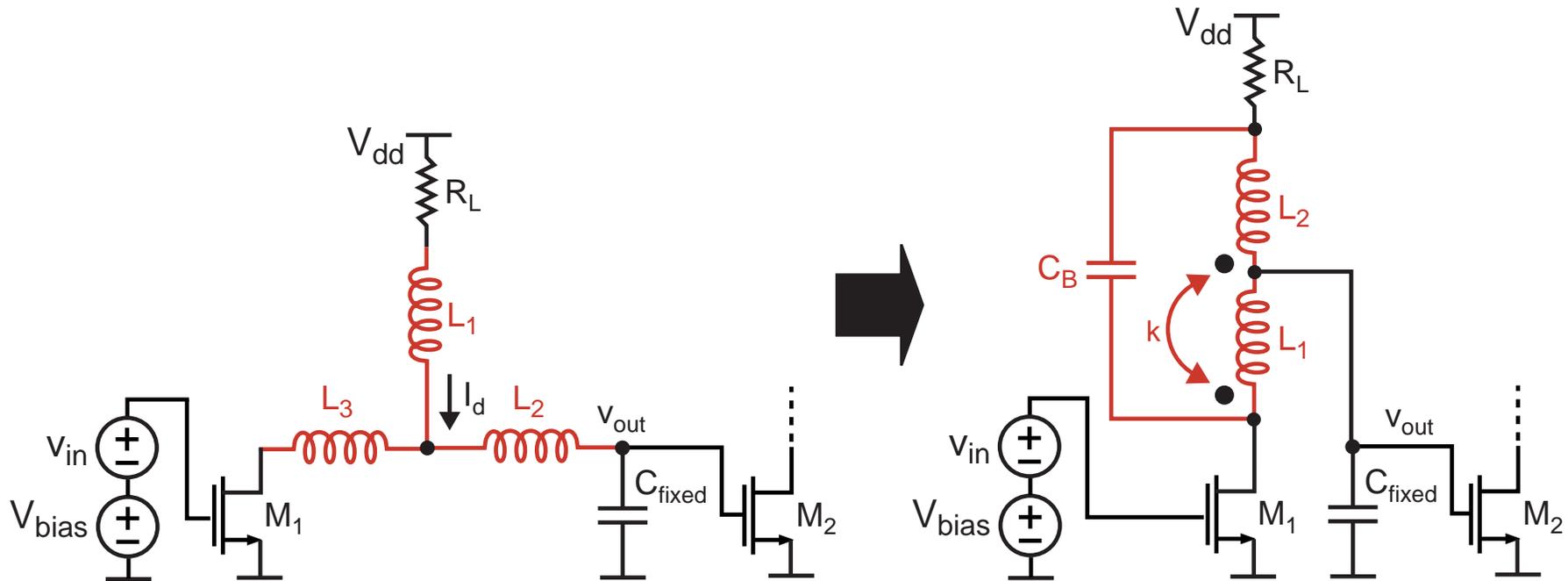
- Inductors are expensive with respect to die area
- We can instead achieve bandwidth extension with capacitor
  - Idea: degenerate gain at low frequencies, remove degeneration at higher frequencies (i.e., create a zero)
- Issues:
  - Must increase  $R_L$  to keep same gain (lowers pole)
  - Lowers achievable gate voltage bias (lowers device  $f_t$ )

# Back to Inductors – Shunt and Series Peaking



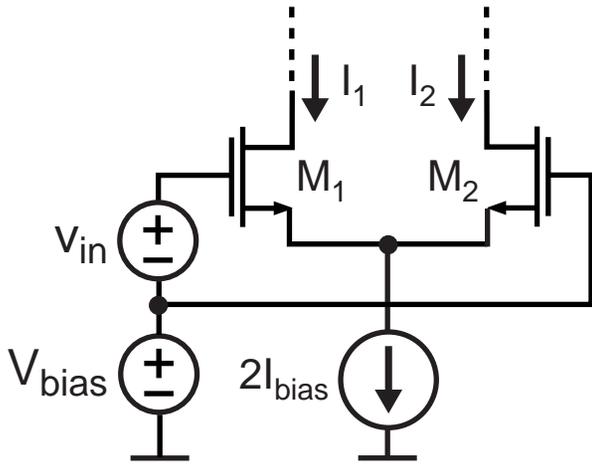
- **Combine shunt peaking with a series inductor**
  - **Bandwidth extension by converting to a second order filter response**
    - Can be designed for proper peaking
- **Increases delay of amplifier**

# T-Coil Bandwidth Enhancement



- **Uses coupled inductors to realize T inductor network**
  - Works best if capacitance at drain of  $M_1$  is much less than the capacitance being driven at the output load
- See Chap. 8 of Tom Lee's book (pp 187-191) for analysis
- See S. Galal, B. Ravazi, "10 Gb/s Limiting Amplifier and Laser/Modulator Driver in 0.18 $\mu$  CMOS", ISSCC 2003, pp 188-189 and "Broadband ESD Protection ...", pp. 182-183

# Bandwidth Enhancement With $f_t$ Doublers



- A MOS transistor has  $f_t$  calculated as

$$2\pi f_t = \frac{g_m}{C_{gs} + C_{gd}} \approx \frac{g_m}{C_{gs}}$$

- $f_t$  doubler amplifiers attempt to increase the ratio of transconductance to capacitance

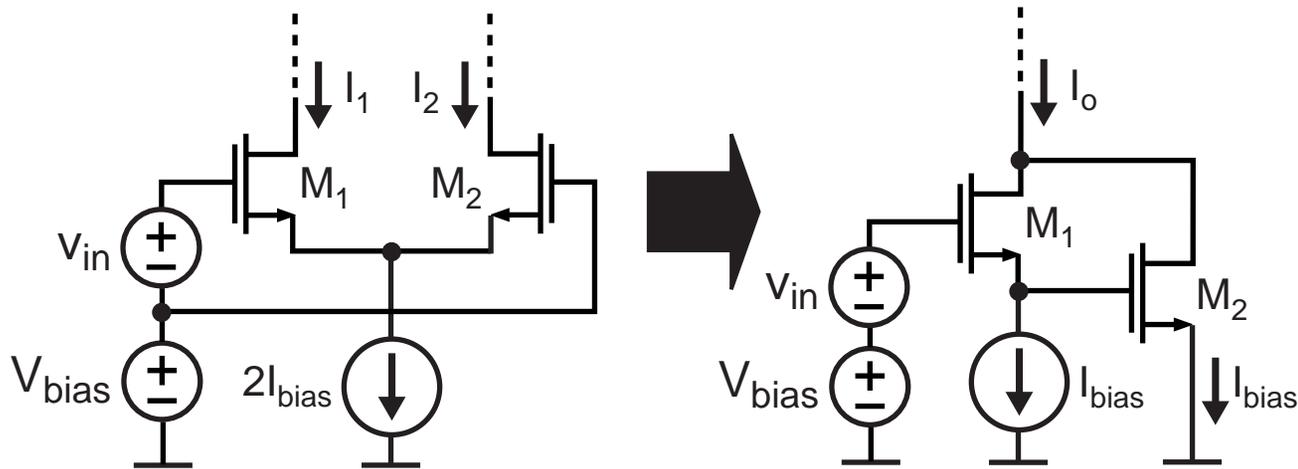
- We can make the argument that differential amplifiers are  $f_t$  doublers

- Capacitance seen by  $V_{in}$  for single-ended input:  $C_{gs}/2$
- Difference in current:

$$i_2 - i_1 = \frac{v_{in}}{2} g_m - \left( -\frac{v_{in}}{2} \right) g_m = v_{in} g_m$$

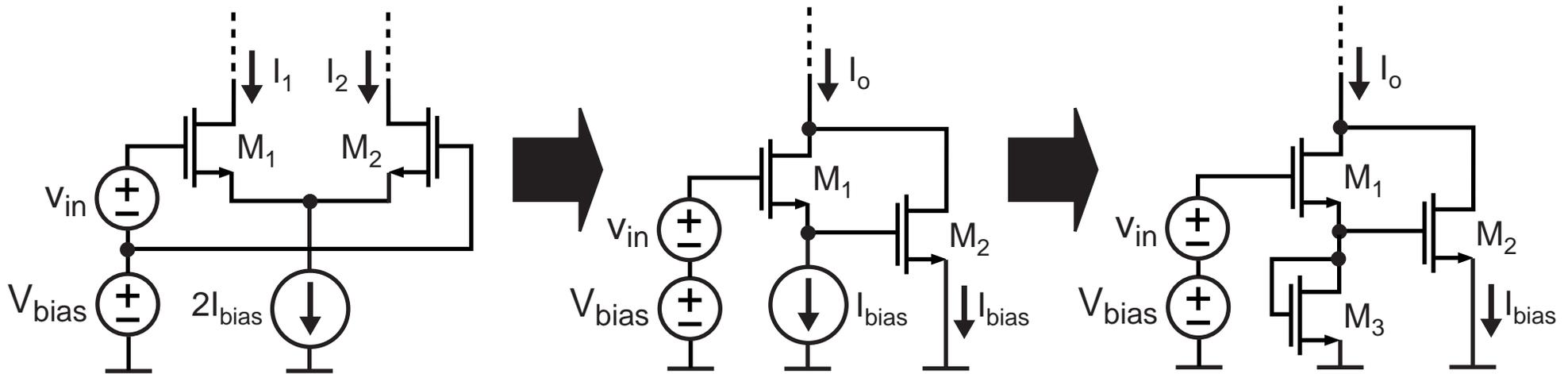
- Transconductance to Cap ratio is doubled:  $\frac{2g_m}{C_{gs}}$

# Creating a Single-Ended Output



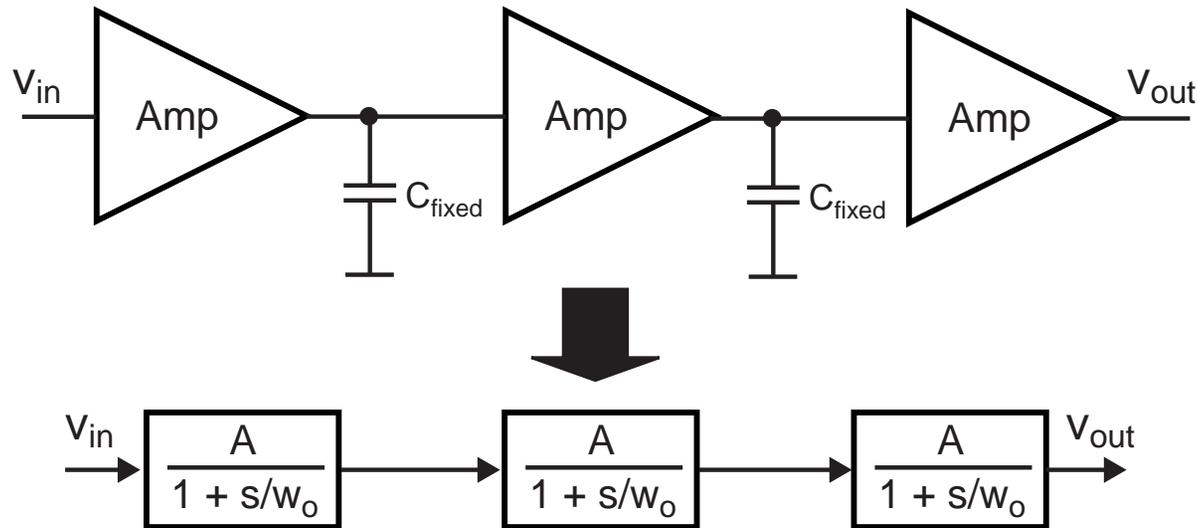
- **Input voltage is again dropped across two transistors**
  - Ratio given by voltage divider in capacitance
    - Ideally is  $\frac{1}{2}$  of input voltage on  $C_{gs}$  of each device
- **Input voltage source sees the series combination of the capacitances of each device**
  - Ideally sees  $\frac{1}{2}$  of the  $C_{gs}$  of  $M_1$
- **Currents of each device add to ideally yield ratio:  $\frac{2g_m}{C_{gs}}$**

## Creating the Bias for $M_2$



- **Use current mirror for bias**
  - Inspired by bipolar circuits (see Tom Lee's book, page 198)
- **Need to set  $V_{bias}$  such that current through  $M_1$  has the desired current of  $I_{bias}$** 
  - The current through  $M_2$  will ideally match that of  $M_1$
- **Problem: achievable bias voltage across  $M_1$  (and  $M_2$ ) is severely reduced (thereby reducing effective  $f_t$  of device)**
  - Do  $f_t$  doublers have an advantage in CMOS?

# Increasing Gain-Bandwidth Product Through Cascading



- We can significantly increase the gain of an amplifier by cascading  $n$  stages

$$\Rightarrow \frac{v_{out}}{v_{in}} = \left( \frac{A}{1 + s/w_0} \right)^n = A^n \frac{1}{(1 + s/w_0)^n}$$

- Issue – bandwidth degrades, but by how much?

# Analytical Derivation of Overall Bandwidth

- The overall 3-db bandwidth of the amplifier is where

$$\left| \frac{v_{out}}{v_{in}} \right| = \left| \frac{A}{1 + j\omega_1/\omega_o} \right|^n = \frac{A^n}{\sqrt{2}}$$

- $\omega_1$  is the overall bandwidth
- $A$  and  $\omega_o$  are the gain and bandwidth of each section

$$\Rightarrow \left( \frac{A}{\sqrt{1 + (\omega_1/\omega_o)^2}} \right)^n = \frac{A^n}{\sqrt{2}}$$

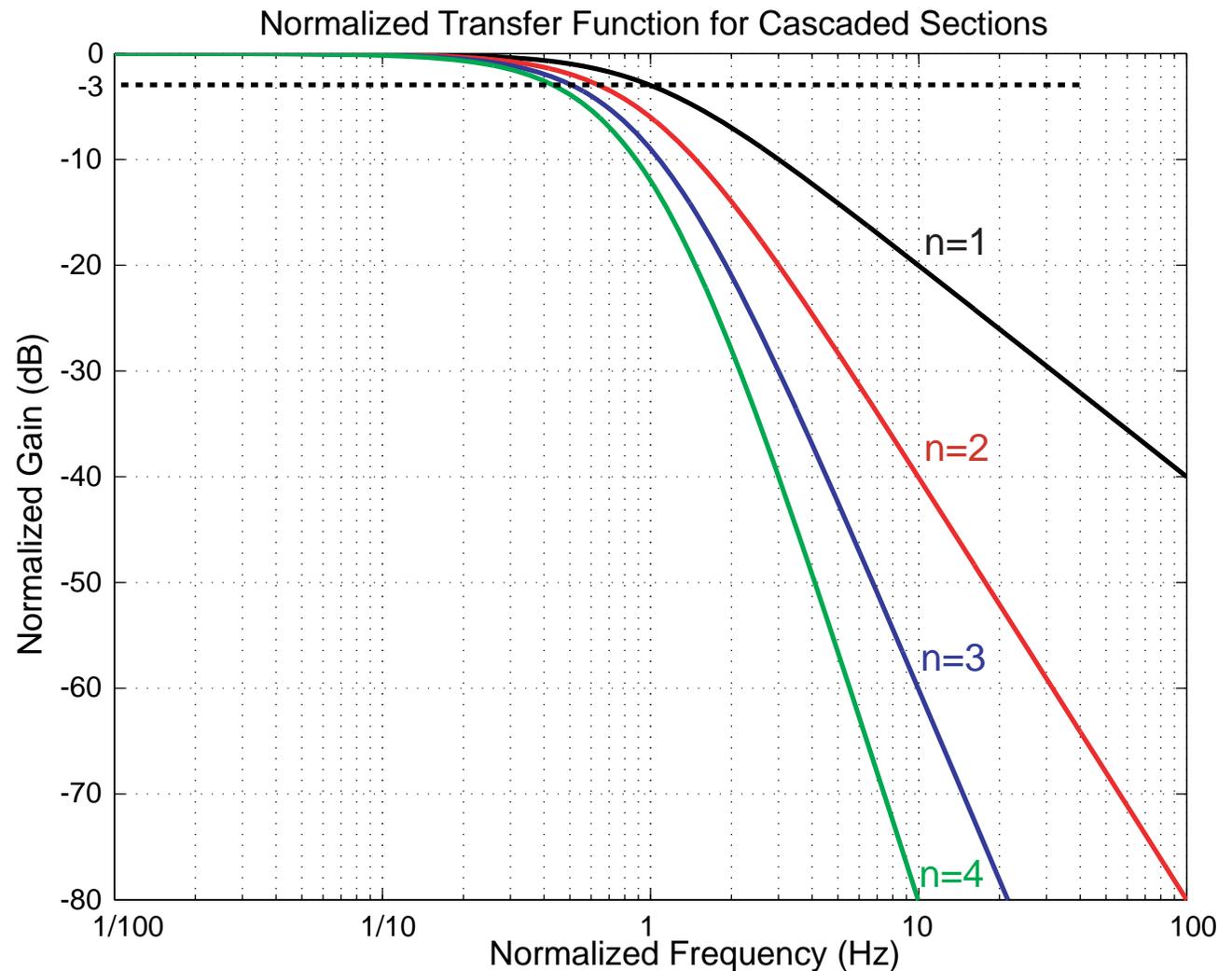
$$\Rightarrow \left( 1 + (\omega_1/\omega_o)^2 \right)^n = 2$$

$$\Rightarrow \omega_1 = \omega_o \sqrt{2^{1/n} - 1}$$

- **Bandwidth decreases much slower than gain increases!**
  - Overall gain bandwidth product of amp can be increased!

# Transfer Function for Cascaded Sections

$$H(f) = \left| \frac{1}{1 + j2\pi f} \right|^n$$



# Choosing the Optimal Number of Stages

- To first order, there is a constant gain-bandwidth product for each stage

$$\Rightarrow Aw_o = w_t \Rightarrow w_o = w_t/A$$

- Increasing the bandwidth of each stage requires that we lower its gain
- Can make up for lost gain by cascading more stages
- We found that the overall bandwidth is calculated as

$$w_1 = w_o \sqrt{2^{1/n} - 1} = \frac{w_t}{A} \sqrt{2^{1/n} - 1}$$

- Assume that we want to achieve gain  $G$  with  $n$  stages

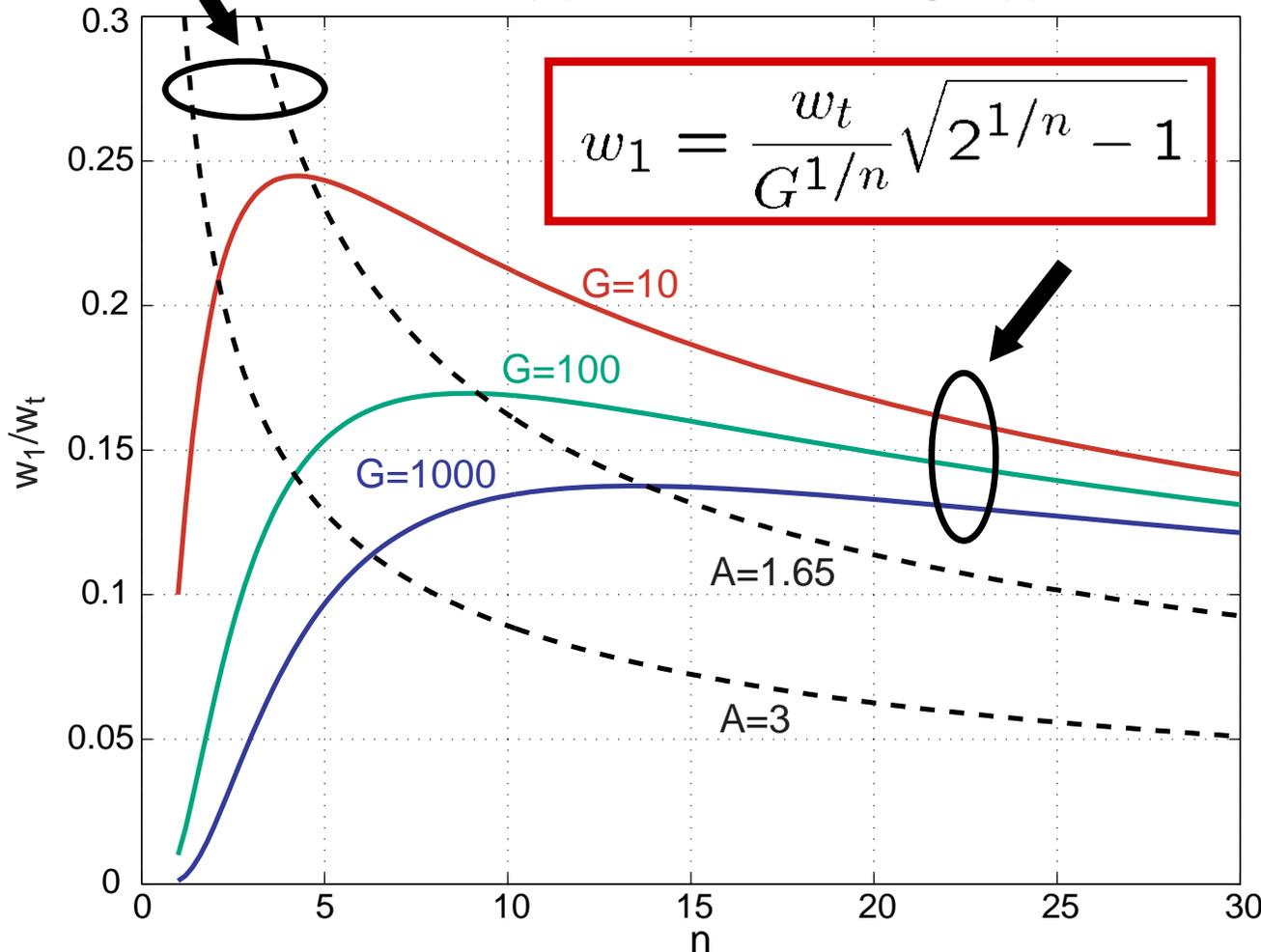
$$\Rightarrow A = G^{1/n} \Rightarrow w_1 = \frac{w_t}{G^{1/n}} \sqrt{2^{1/n} - 1}$$

- From this, optimum gain  $\approx \text{sqrt}(e) = 1.65$ 
  - See Tom Lee's book, pp 207-211

# Achievable Bandwidth Versus $G$ and $n$

$$\frac{w_t}{A} \sqrt{2^{1/n} - 1}$$

Achievable Bandwidth (Normalized to  $f_t$ )  
Versus Gain ( $G$ ) and Number of Stages ( $n$ )



- Optimum gain per stage is about 1.65

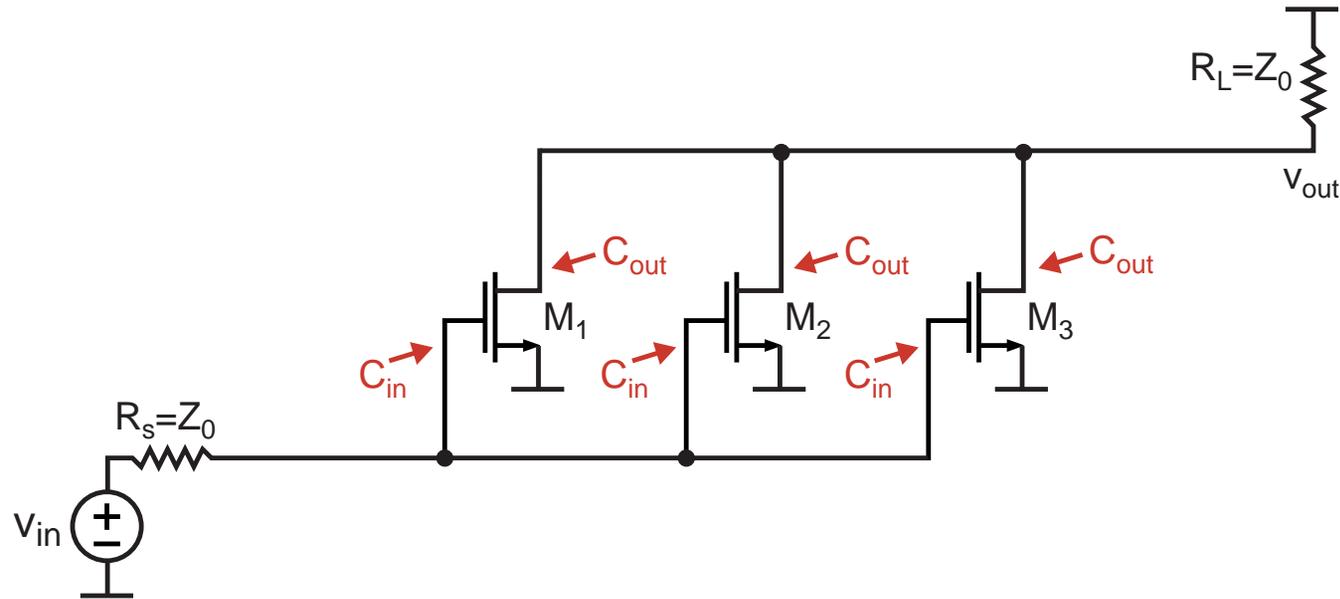
- Note that gain per stage derived from plot as

$$A = G^{1/n}$$

- Maximum is fairly soft, though

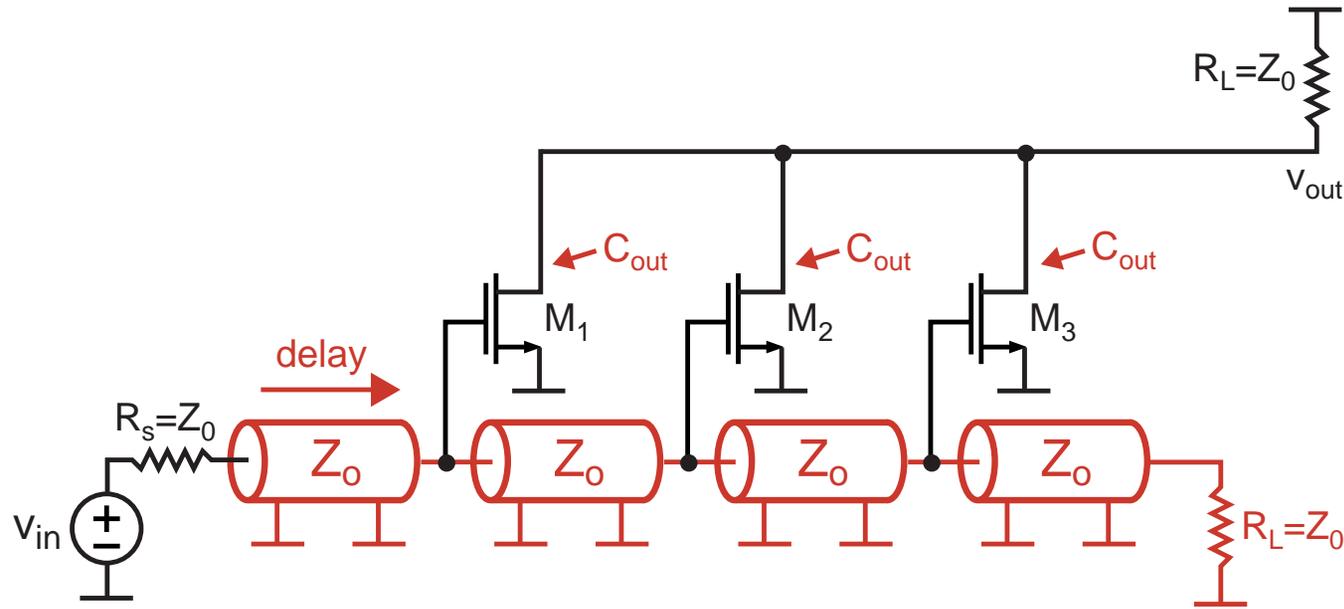
- Can dramatically lower power (and improve noise) by using larger gain per stage

# Motivation for Distributed Amplifiers



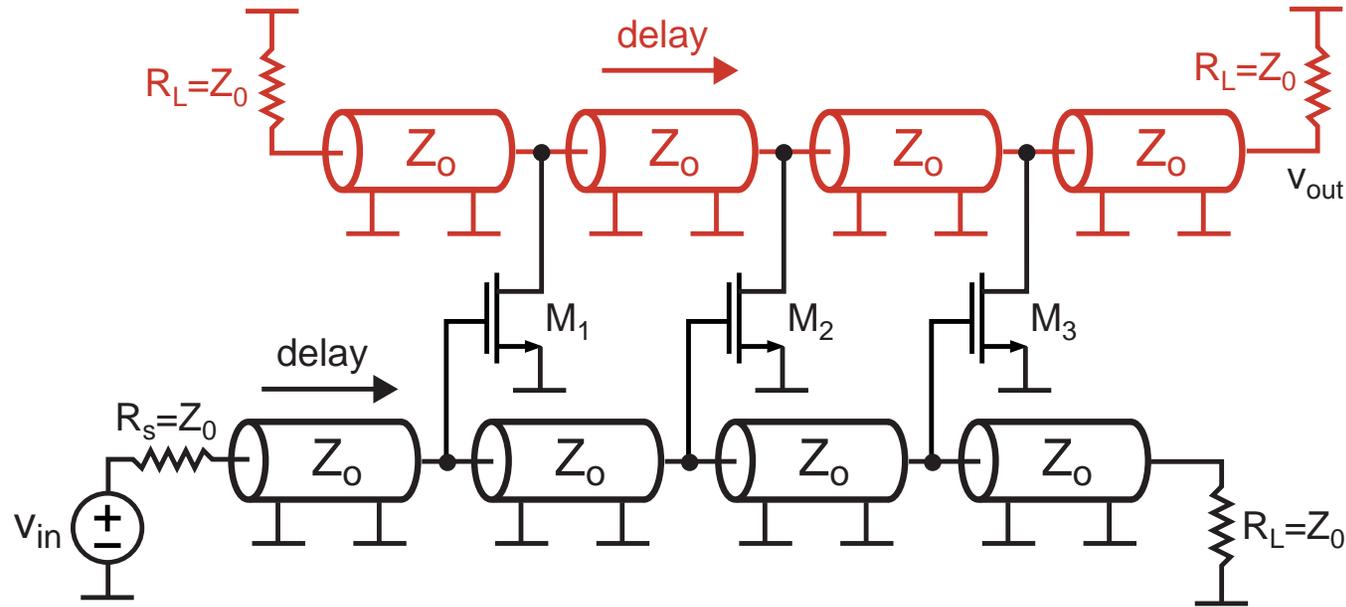
- We achieve higher gain for a given load resistance by increasing the device size (i.e., increase  $g_m$ )
  - Increased capacitance lowers bandwidth
    - We therefore get a relatively constant gain-bandwidth product
- We know that transmission lines have (ideally) infinite bandwidth, but can be modeled as LC networks
  - Can we lump device capacitances into transmission line?

# Distributing the Input Capacitance



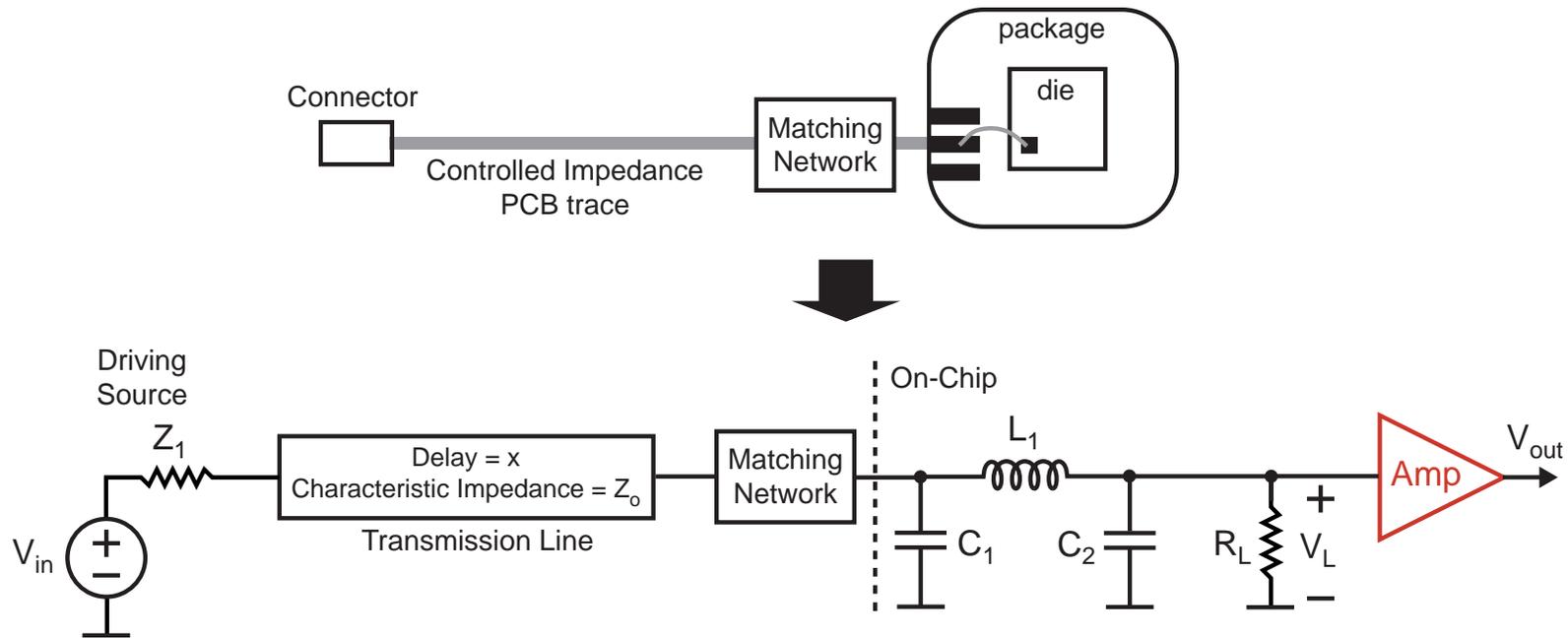
- **Lump input capacitance into LC network corresponding to a transmission line**
  - Signal ideally sees a real impedance rather than an RC lowpass
  - Often implemented as lumped networks such as T-coils
  - We can now trade delay (rather than bandwidth) for gain
- **Issue: outputs are delayed from each other**

# Distributing the Output Capacitance



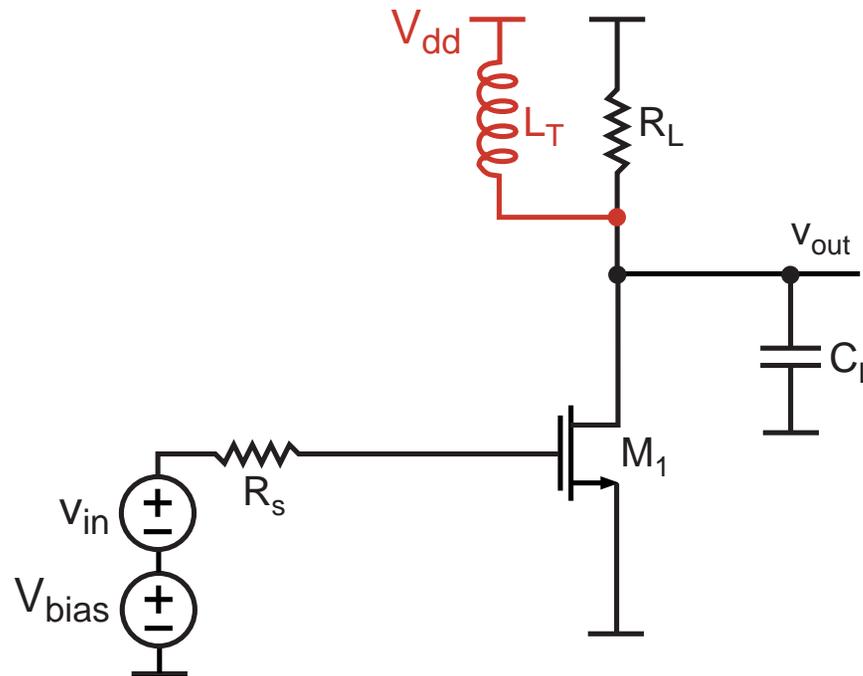
- **Delay the outputs same amount as the inputs**
  - Now the signals match up
  - We have also distributed the output capacitance!
- **Benefit – high bandwidth**
- **Negatives – high power, poorer noise performance, expensive in terms of chip area**
  - Each transistor gain is adding rather than multiplying!

# Narrowband Amplifiers



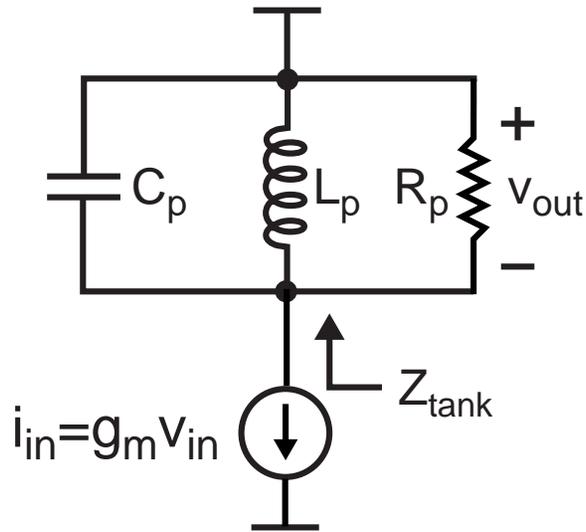
- For wireless systems, we are interested in conditioning and amplifying the signal over a narrow frequency range centered at a high frequency
  - Allows us to apply narrowband transformers to create matching networks
- Can we take advantage of this fact when designing the amplifier?

# Tuned Amplifiers



- Put inductor in parallel across  $R_L$  to create bandpass filter
  - It will turn out that the gain-bandwidth product is roughly conserved regardless of the center frequency!
    - Assumes that center frequency (in Hz)  $\ll f_t$
- To see this and other design issues, we must look closer at the parallel resonant circuit

# Tuned Amp Transfer Function About Resonance



- Amplifier transfer function

$$\frac{v_{out}}{v_{in}} = g_m Z_{tank}(s) = \frac{g_m}{Y_{tank}(s)}$$

- Note that conductances add in parallel

$$Y_{tank}(s) = \frac{1}{R_p} + \frac{1}{sL_p} + sC_p$$

- Evaluate at  $s = j\omega$

$$Y_{tank}(\omega) = \frac{1}{R_p} - \frac{j}{\omega L_p} + j\omega C_p = \frac{1}{R_p} + \frac{j}{\omega L_p} (-1 + \omega^2 L_p C_p)$$

- Look at frequencies about resonance:  $\omega = \omega_o + \Delta\omega$

$$\begin{aligned} \Rightarrow Y_{tank}(\Delta\omega) &= \frac{1}{R_p} + \frac{j}{(\omega_o + \Delta\omega)L_p} (-1 + (\omega_o + \Delta\omega)^2 L_p C_p) \\ &\approx \frac{1}{R_p} + \frac{j}{\omega_o L_p} (-1 + \omega_o^2 L_p C_p + 2\omega_o \Delta\omega L_p C_p) \end{aligned}$$

# Tuned Amp Transfer Function About Resonance (Cont.)

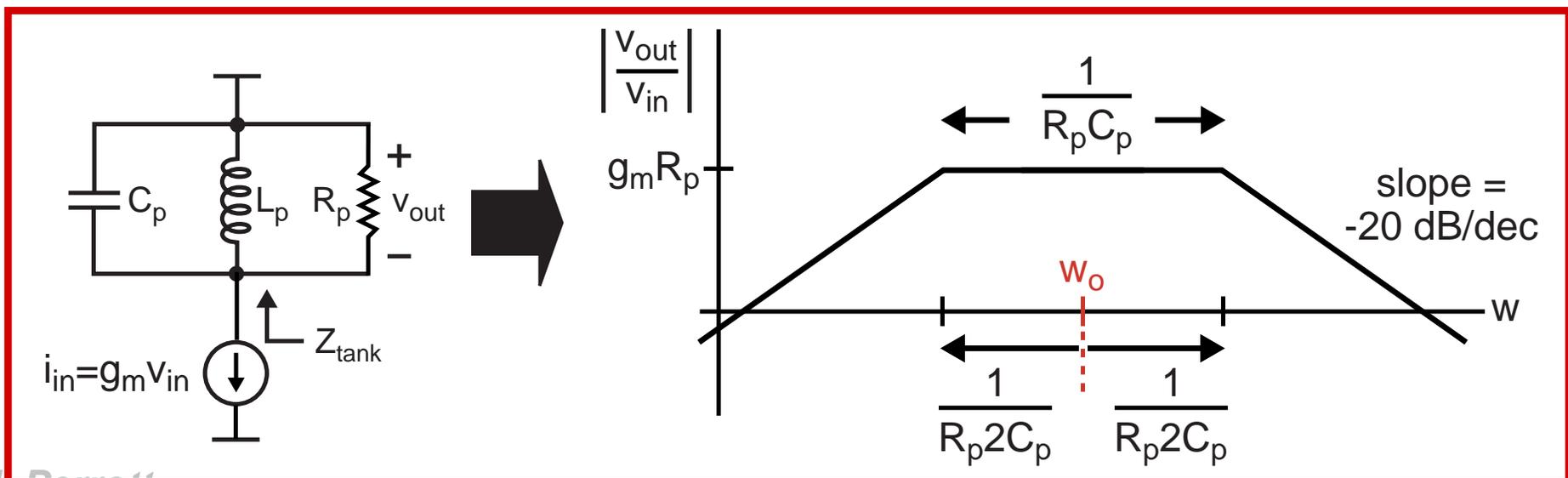
- From previous slide

$$Y_{tank}(\Delta\omega) \approx \frac{1}{R_p} + \frac{j}{\omega_o L_p} \left( \underbrace{-1 + \omega_o^2 L_p C_p}_{=0} + 2\omega_o \Delta\omega L_p C_p \right)$$

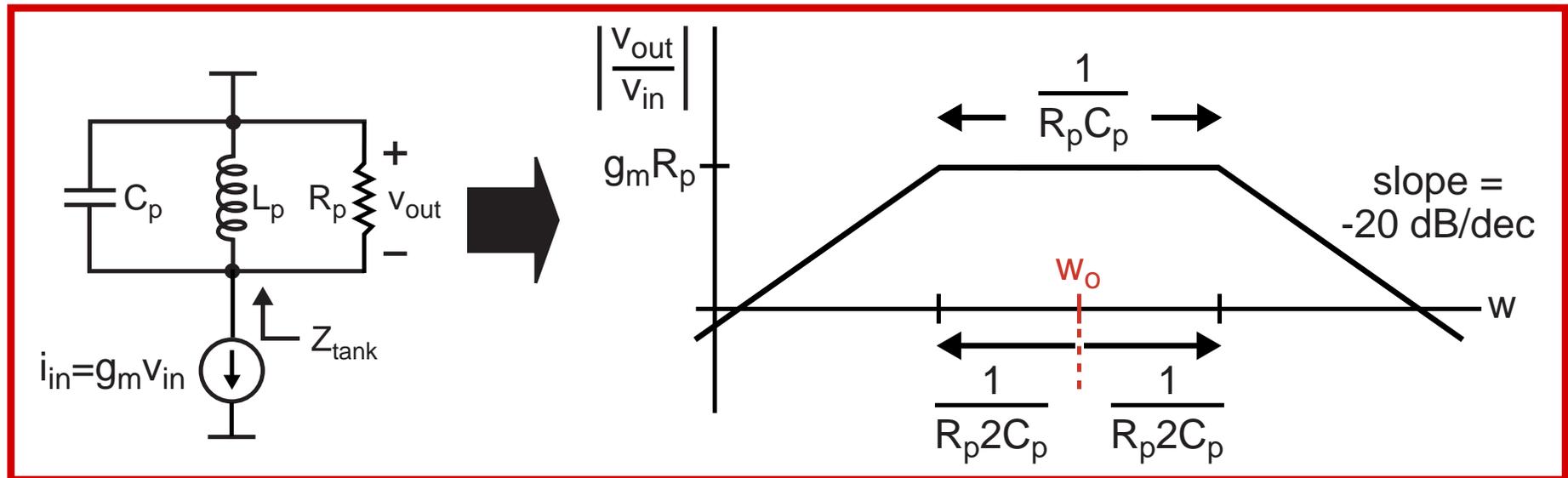
$$\approx \frac{1}{R_p} + \frac{j}{\omega_o L_p} (2\omega_o \Delta\omega L_p C_p) = \frac{1}{R_p} + j \Delta\omega 2C_p$$

- Simplifies to RC circuit for bandwidth calculation!

$$Z_{tank}(\Delta\omega) \approx R_p \parallel \frac{1}{j \Delta\omega 2C_p}$$



# Gain-Bandwidth Product for Tuned Amplifiers

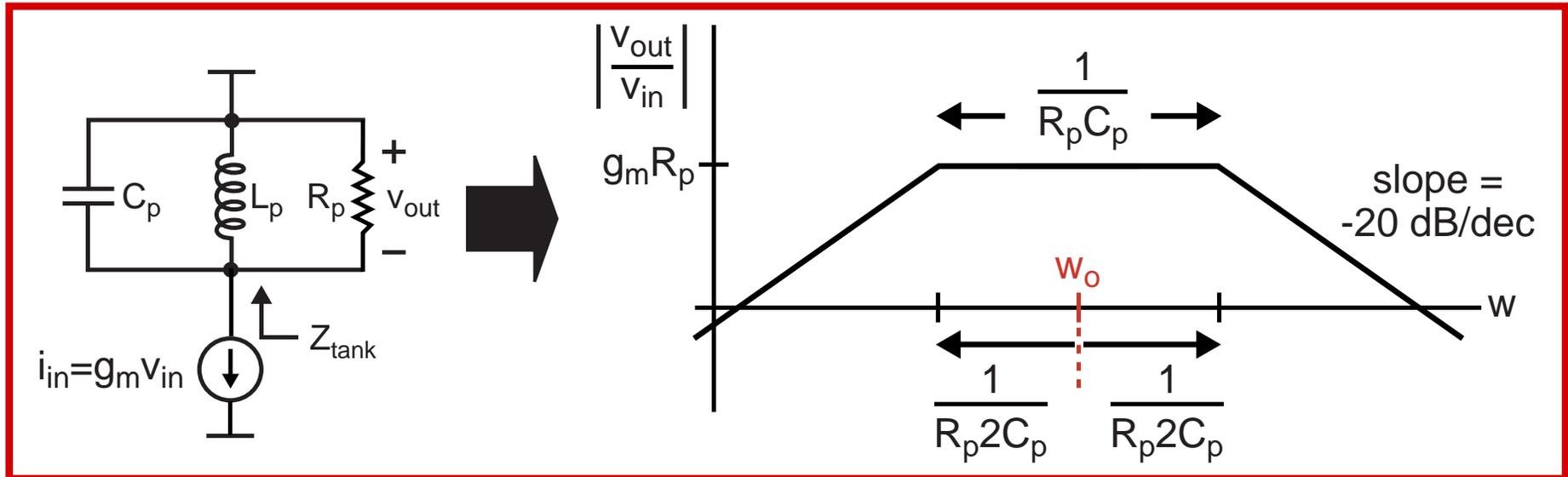


- The gain-bandwidth product:

$$G \cdot BW = g_m R_p \frac{1}{R_p C_p} = \frac{g_m}{C_p}$$

- The above expression is independent of center frequency!
  - In practice, we need to operate at a frequency less than the  $f_t$  of the device

# The Issue of Q



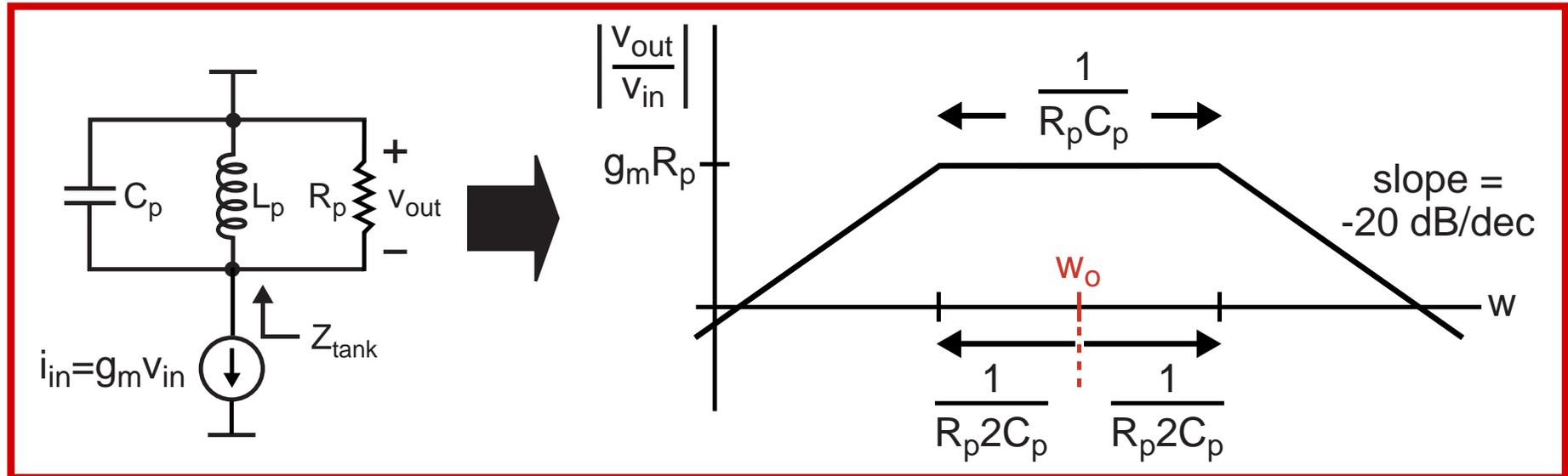
- **By definition**  $Q = w \frac{\text{energy stored}}{\text{average power dissipated}}$

- **For parallel tank (see Tom Lee's book, pp 88-89)**

at resonance:  $Q = \frac{R_p}{\omega_0 L_p} = \omega_0 R_p C_p$

- **Comparing to above:**  $Q = \omega_0 R_p C_p = \frac{\omega_0}{1/(R_p C_p)} = \boxed{\frac{\omega_0}{BW}}$

# Design of Tuned Amplifiers



## ■ Three key parameters

- Gain =  $g_m R_p$
- Center frequency =  $\omega_0$
- $Q = \omega_0 / BW$

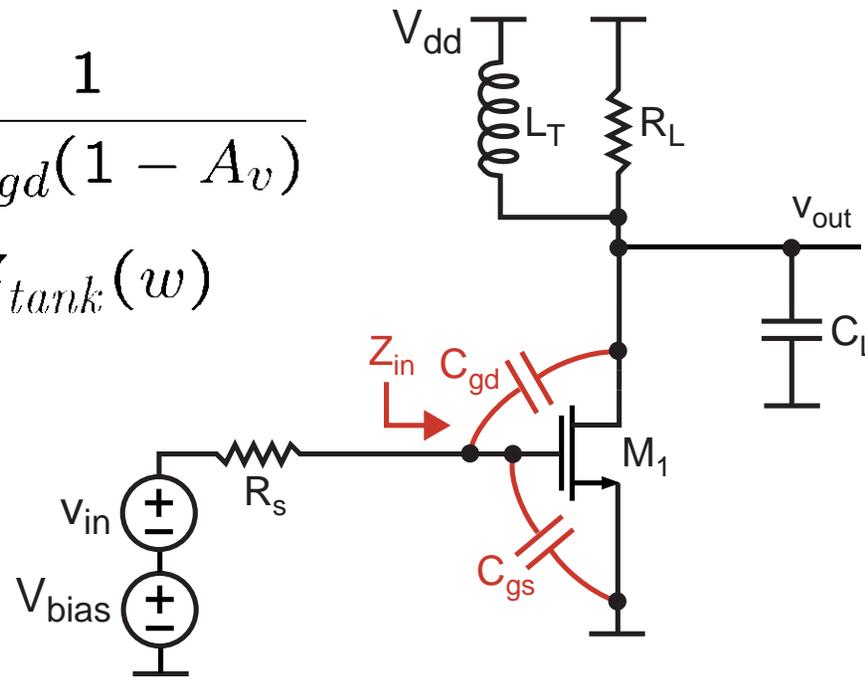
## ■ Impact of high Q

- Benefit: allows achievement of high gain with low power
- Problem: makes circuit sensitive to process/temp variations

## Issue: $C_{gd}$ Can Cause Undesired Oscillation

$$Z_{in}(w) = \frac{1}{jwC_{gs}} \parallel \frac{1}{jwC_{gd}(1 - A_v)}$$

where  $A_v = -g_m Z_{tank}(w)$



- At frequencies below resonance, tank looks inductive

$$A_v \approx -g_m(jwL) \Rightarrow Z_{in}(w) \approx \frac{1}{jwC_{gs}} \parallel \frac{1}{jwC_{gd}(1 + g_m(jwL))}$$

$$\Rightarrow Z_{in}(w) \approx \frac{1}{jwC_{gs}} \parallel \frac{1}{jwC_{gd} - w^2 g_m C_{gd} L}$$

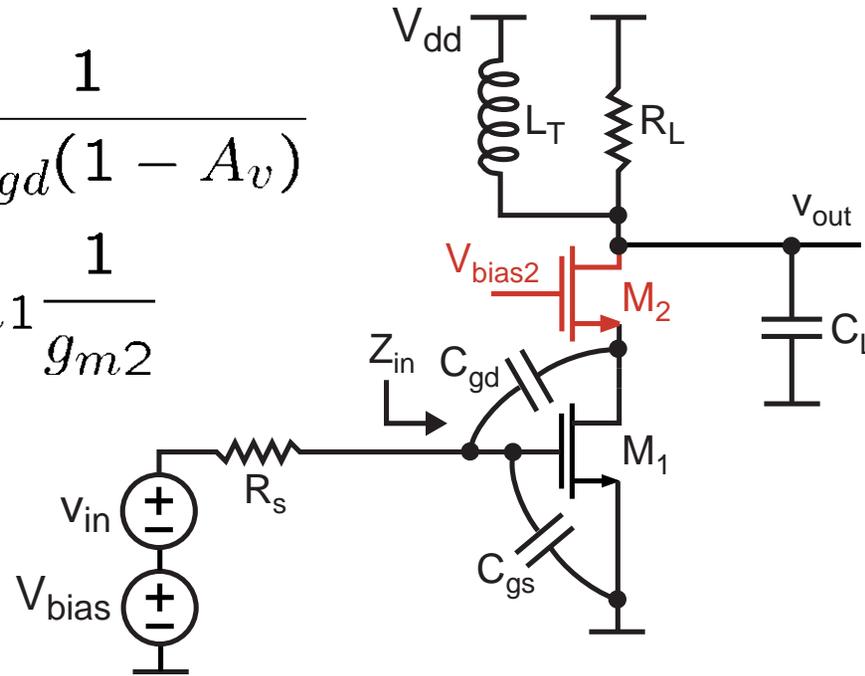
$$\Rightarrow Z_{in}(w) \approx \frac{1}{jwC_{gs}} \parallel \frac{1}{jwC_{gd}} \parallel \frac{-1}{w^2 g_m C_{gd} L}$$

**Negative Resistance!**

## Use Cascode Device to Remove Impact of $C_{gd}$

$$Z_{in}(w) = \frac{1}{jwC_{gs}} \parallel \frac{1}{jwC_{gd}(1 - A_v)}$$

$$\text{where } A_v = -g_{m1} \frac{1}{g_{m2}}$$

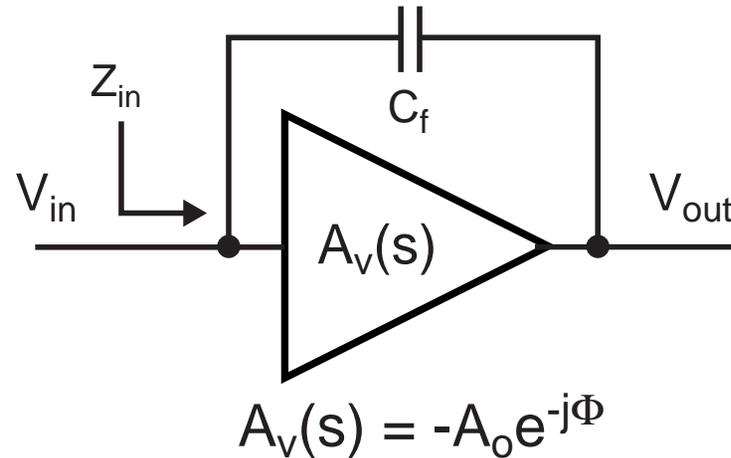


- At frequencies above and below resonance

$$Z_{in}(w) = \frac{1}{jwC_{gs}} \parallel \frac{1}{jwC_{gd}(1 + g_{m1}/g_{m2})}$$

**Purely  
Capacitive!**

# Active Real Impedance Generator

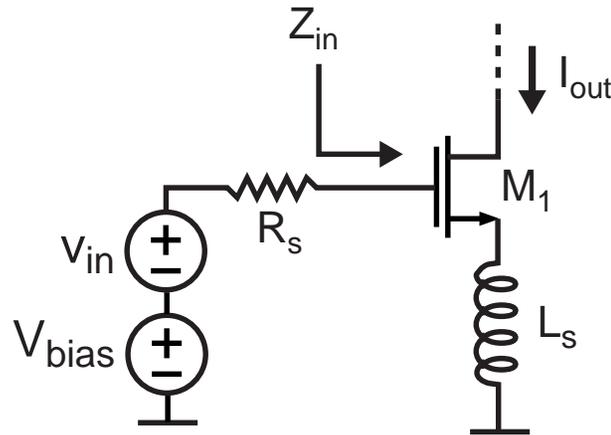


- **Input impedance:**

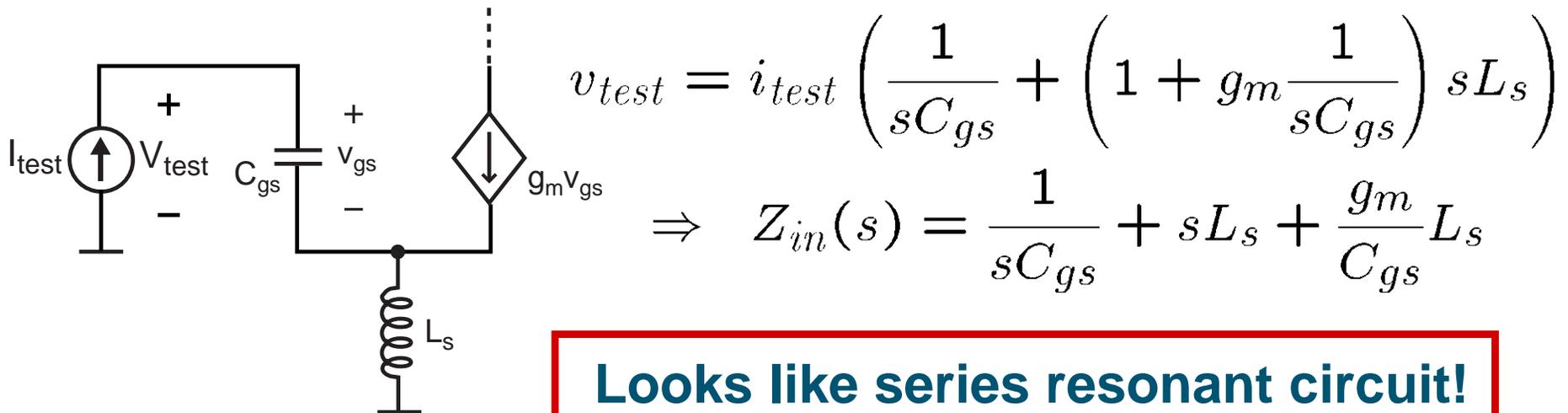
$$\begin{aligned} Z_{in}(\omega) &= \frac{1}{j\omega C_f(1 - A_v)} = \frac{1}{j\omega C_f(1 + A_o e^{-j\Phi})} \\ &= \frac{1}{j\omega C_f(1 + A_o \cos \Phi) + A_o \omega C_f \sin \Phi} \\ &= \frac{1}{j\omega C_f(1 + A_o \cos \Phi)} \parallel \frac{1}{A_o \omega C_f \sin \Phi} \end{aligned}$$

**Resistive component!**

# This Principle Can Be Applied To Impedance Matching

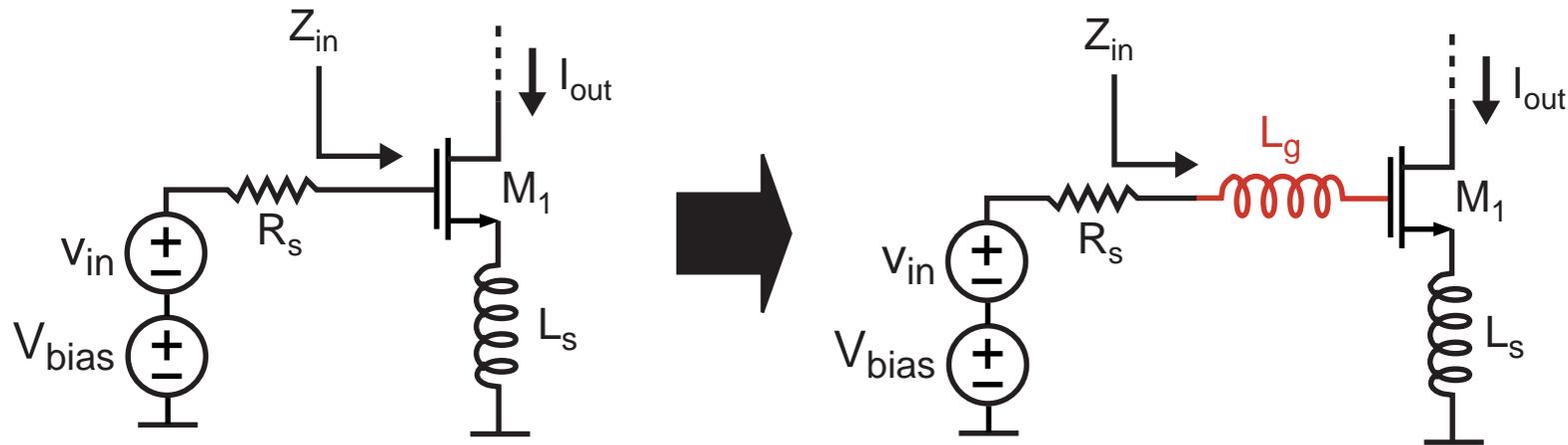


- We will see that it's advantageous to make  $Z_{in}$  real without using resistors
  - For the above circuit (ignoring  $C_{gd}$ )



**Looks like series resonant circuit!**

# Use A Series Inductor to Tune Resonant Frequency



- Calculate input impedance with added inductor

$$Z_{in}(s) = \frac{1}{sC_{gs}} + s(L_s + L_g) + \frac{g_m}{C_{gs}}L_s$$

- Often want purely resistive component at frequency  $\omega_0$ 
  - Choose  $L_g$  such that resonant frequency =  $\omega_0$

$$\text{i.e., want } \frac{1}{\sqrt{(L_s + L_g)C_{gs}}} = \omega_0$$